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Lena Chang

Associated Professor, Department of Merchant Marine, National Taiwan Ocean University, Taiwan, R.O.C.

Chung-Fan Twu

Graduate Student, Department of Merchant Marine, National Taiwan Ocean University, Taiwan, R.O.C.

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THE ESTIMATION OF DIRECTION-OF-ARRIVALS OF WIDEBAND SOURCES BY SIGNAL SUBSPACE FOCUSING APPROACH

Lena Chang* and Chung-Fan Twu**

Keywords: Signal subspace, Focusing matrix, Direction-of-arrival (DOA), Wideband.

ABSTRACT

A novel signal subspace focusing (SSF) approach for the wideband array processing is proposed in this paper. The method is based on the transformation of the signal subspaces by using focusing matrices. The focusing matrix is designed to align the signal subspaces for different frequencies in the bandwidth of the sources, and is constructed without the preliminary angle estimation. Hence, the SSF can avoid the inherent sensitivity to focusing error. Simulation results validate the effectiveness of the SSF in the estimation of the direction-of-arrivals (DOAs) of wideband sources.

INTRODUCTION

The Coherent Signal-subspace Method (CSM) [1] has been proposed for the estimation of the direction-of-arrivals (DOAs) of multiple wideband sources received by the passive array. In the CSM, the estimated spectrum density matrices of each frequency bin within the received bandwidth are first transformed onto a common frequency (usually the receiver center frequency) by focusing matrices, and then averaged to obtain a focused spectrum density matrix. Although the CSM is very effective in the wideband signal detection and estimation, it suffers from the construction of the focusing matrices which require a set of preliminary DOAs estimation by low resolution methods, such as beamforming or spectrum paradigm. If these preliminary DOAs estimation are inappropriately selected, the CSM often results in an estimation error in focusing matrices, especially in

multi-group signals. Thus, the estimation bias increases with the deviation of the focusing points from the true DOAs. Several focusing matrices have been suggested to construct effective focusing for the CSM. These matrices include rotation signal-subspace (RSS) [2], array manifold interpolation (AMI) [3], unitary constrained array manifold focusing (UCAM) [4] and others [5,6].

In this paper, we introduce a new focusing method, named signal subspace focusing (SSF), for the DOAs estimation of wideband sources. Similar to the CSM, the SSF transforms the signal subspace, which corresponds to the spectrum density matrix, at each frequency bin onto the focusing subspace (usually the signal subspace at receiver center frequency) by using focusing matrices. The focusing matrices are unitary and are chosen to minimize the distance between the focusing subspace and the signal subspace at each frequency bin. In contrast to the CSM, in which the focusing matrices are determined by transforming the directional matrix at each frequency bin to that at focusing frequency, the focusing matrices of the SSF is formulated without the preliminary estimation of the source direction. Thus, the DOAs estimation of the proposed method is insensitive to focusing error. Simulation results validate the performance of the proposed SSF method is better than that of the CSM.

This paper is organized as follows. Section II describes the data model of wideband sources and reviews the CSM method. Section III presents the SSF method. Computer simulations are included in Section IV. Finally, Section V contains the conclusions.

BACKGROUND

This section contains a brief review on the data model and the CSM.

Data Model

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*Associated Professor, Department of Merchant Marine, National Taiwan Ocean University, Taiwan, R.O.C.

**Graduate Student, Department of Merchant Marine, National Taiwan Ocean University, Taiwan, R.O.C.

Consider a p -element arbitrary geometry array illuminated by q wideband sources. The source signals are band limited to a common frequency band with bandwidth B . The signal received at the m -th sensor can be expressed as

$$x_m(t) = \sum_{i=1}^q a_{mi} s_i(t - \tau_{mi}) + n_m(t), \quad (1)$$

where a_{mi} is the complex gain of the m -th sensor with respect to the i -th source, τ_{mi} is the propagation delay for the i -th source at the sensor m with respect to the reference point of the array, and $n_m(t)$ is the additive noise at the sensor m . For a uniform linear array $\tau_{mi} = (m-1) \frac{d}{c} \sin \theta_i$, where d is the spacing between the consecutive sensors, c is the propagation velocity, θ_i is the DOA for the i -th source and the reference point is at the first sensor.

The received signal $x_m(t)$ can be represented by its Fourier components in the frequency domain. The discrete Fourier transform of $x_m(t)$ over the snapshot interval T consists of K Fourier components, $X_m(f_k)$, given by

$$X_m(f_k) = \sum_{i=1}^q a_{mi} e^{-j2\pi f_k \tau_{mi}} S_i(f_k) + N_m(f_k), \quad k = 1, \dots, K, \quad (2)$$

where $S_i(f_k)$ and $N_m(f_k)$ denote the k -th Fourier components of the $s_i(t)$ and $n_m(t)$, respectively. The k -th Fourier components corresponding to the array measurements $x_1(t)$, $x_2(t)$, ..., $x_p(t)$ can be expressed as a vector form:

$$\mathbf{X}(f_k) = \begin{bmatrix} X_1(f_k) \\ X_2(f_k) \\ \vdots \\ X_p(f_k) \end{bmatrix} = \mathbf{A}(\theta, f_k) \mathbf{S}(f_k) + \mathbf{N}(f_k), \quad (3)$$

where $\mathbf{A}(\theta, f_k)$ is a $p \times q$ matrix and represents the array direction matrix corresponding to frequency f_k , given by

$$\mathbf{A}(\theta, f_k) = [a(\theta_1, f_k) \ a(\theta_2, f_k) \ \dots \ a(\theta_q, f_k)], \quad (4)$$

$\mathbf{S}(f_k) = [S_1(f_k), S_2(f_k), \dots, S_q(f_k)]^T$ and $\mathbf{N}(f_k) = [N_1(f_k), N_2(f_k), \dots, N_p(f_k)]^T$ denote the vectors formed by the Fourier components of signal and noise at frequency f_k , respectively. In (4), $a(\theta_i, f_k)$ represents the direction vector of i -th sources at frequency f_k ,

$$a(\theta_i, f_k) = \begin{bmatrix} a_{1i} e^{-j2\pi f_k \tau_{1i}} \\ a_{2i} e^{-j2\pi f_k \tau_{2i}} \\ \vdots \\ a_{pi} e^{-j2\pi f_k \tau_{pi}} \end{bmatrix}, \quad i = 1, 2, \dots, q.$$

Suppose the noise $\mathbf{N}(f_k)$ is independent of the source signal $\mathbf{S}(f_k)$ and has zero mean with known noise spectrum density matrix $P_{\eta}(f_k)$, but unknown spectrum level $\sigma^2(f_k)$. Hence, the spectrum density matrix of the array output is given by

$$P_X(f_k) = E[\mathbf{X}(f_k) \mathbf{X}^H(f_k)] = \mathbf{A}(\theta, f_k) P_S(f_k) \mathbf{A}^H(\theta, f_k) + \sigma^2(f_k) P_{\eta}(f_k). \quad (5)$$

In (5), $P_S(f_k)$ is the source spectrum density matrix which may be singular in the presence of multipath propagation.

In practice, $P_X(f_k)$ is unavailable and is estimated by a sufficiently long duration of sensor output. The observation time T is sectioned into L snapshots of duration T_o each. For sufficient large T_o , we may estimate $P_X(f_k)$ by time averaging,

$$\hat{P}_X(f_k) = \frac{1}{L} \sum_{\ell=1}^L \mathbf{X}_{\ell}(f_k) \mathbf{X}_{\ell}^H(f_k), \quad k = 1, 2, \dots, K, \quad (6)$$

where $\mathbf{X}_{\ell}(f_k)$ is the Fourier transform component at frequency f_k of observations on snapshot ℓ . The problem formulation leads to the following objective: given the data set $\mathbf{X}_{\ell}(f_k)$ $\ell = 1, \dots, L$, $k = 1, \dots, K$, estimate the DOAs $\theta_1, \dots, \theta_q$, of the wideband sources.

Coherent Signal-subspace Method (CSM)

The objective of the CSM is to transform the sensor output $\mathbf{X}(f_k)$ so that the direction matrix is constant for all frequencies within the common bandwidth of the sources. In the CSM, the observation vector $\mathbf{X}(f_k)$ at different frequency bin is transformed into a new vector as

$$\mathbf{Y}(f_k) = T(f_k) \mathbf{X}(f_k), \quad (7)$$

where $T(f_k)$ is the focusing matrix and satisfies

$$T(f_k) \mathbf{A}(\theta, f_k) = \mathbf{A}(\theta, f_o), \quad k = 1, 2, \dots, K. \quad (8)$$

In (8), $\mathbf{A}(\theta, f_o)$ is the focusing direction matrix. From (5), we get the spectrum density matrix of the transformed vector $\mathbf{Y}(f_k)$,

$$\begin{aligned} P_Y(f_k) &= E[\mathbf{Y}(f_k) \mathbf{Y}^H(f_k)] \\ &= T(f_k) P_X(f_k) T^H(f_k) \\ &= \mathbf{A}(\theta, f_o) P_S(f_k) \mathbf{A}^H(\theta, f_o) \\ &\quad + \sigma^2(f_k) T(f_k) P_{\eta}(f_k) T^H(f_k). \end{aligned} \quad (9)$$

Equation (9) indicates the signal subspace alignment procedure which makes the transformed vectors, $\mathbf{Y}(f_k)$, $k = 1, \dots, K$, have the same signal subspace. Then,

combine the spectrum density matrices $P_Y(f_k)$ over the frequency band by an averaging procedure and construct the smoothed spectrum density matrix

$$R_Y = \mathbf{A}(\theta, f_o) R_s \mathbf{A}^H(\theta, f_o) + \sigma^2 R_\eta, \quad (10)$$

where $R_s = \sum_{k=1}^K P_S(f_k)$, σ^2 is the sum of noise spectral level $\sigma^2(f_k)$ across the full bandwidth and $R_\eta = \sum_{k=1}^K \frac{\sigma^2(f_k)}{\sigma^2} T(f_k) P_n(f_k) T^H(f_k)$. Equation (10) indicates the estimating DOAs of the wideband sources can be performed by utilizing any super-resolution signal subspace methods proposed for estimating the DOAs of narrow-band sources, for example, the MUSIC algorithm.

Recently, several focusing matrices have been proposed to construct effective focusing for the CSM, for example the RSS [2] focusing matrices, which can be used in the CSM for estimating DOAs of wideband sources distributed in multiple clusters. In RSS, the focusing matrices are the solutions of the minimization problem

$$\min_{T(f_k)} \|\mathbf{A}(\theta, f_o) - T(f_k) \mathbf{A}(\theta, f_k)\|_F, \quad k = 1, 2, \dots, K, \quad (11)$$

subject to

$$T^H(f_k) T(f_k) = I,$$

where $\|\cdot\|_F$ is the Frobenius matrix norm. Minimization of (11) gives the solution of $T(f_k)$ as

$$T(f_k) = C(f_k) D^H(f_k), \quad (12)$$

where the columns of $C(f_k)$ and $D(f_k)$ are the left and right singular vectors of $\mathbf{A}(\theta, f_k) \mathbf{A}^H(\theta, f_o)$.

However, the focusing matrices in (8) and (12) require the preliminary angle estimation, which will result in the estimation bias for the CSM. To alleviate the performance degradation of the CSM, we will propose a new method for the processing of the wideband sources.

SIGNAL SUBSPACE FOCUSING (SSF)

In this section, we introduce a signal subspace focusing (SSF) method for wideband source estimation. Our method is based on the transformation of the signal subspace corresponding to the spectrum density matrix $P_X(f_k)$ into a signal subspace, named the focusing subspace. The transformation is done by using the focusing matrix, which satisfies

$$T(f_k) E_s(f_k) = E_s(f_o). \quad (13)$$

In (13), $E_s(f_k) = [e_1(f_k), e_2(f_k), \dots, e_q(f_k)]$ and $E_s(f_o) = [e_1(f_o), e_2(f_o), \dots, e_q(f_o)]$, where $e_i(f_k)$ and $e_i(f_o)$, for $i = 1, \dots, q$, are the eigenvectors corresponding to the q larger eigenvalues of $P_X(f_k)$ and $P_X(f_o)$, respectively. [2] has shown that a good focusing matrix is unitary. Hence, the focusing matrix in (13) is chosen to be unitary and satisfies the following constrained minimization problem

$$\min_{T(f_k)} \|E_s(f_o) - T(f_k) E_s(f_k)\|_F, \quad k = 1, 2, \dots, K, \quad (14)$$

subject to

$$T^H(f_k) T(f_k) = I.$$

The solution of (14) can be get as

$$T(f_k) = V(f_k) U^H(f_k). \quad (15)$$

In (15), $V(f_k)$ and $U(f_k)$ are the matrices containing the left and right singular vectors of $E_s(f_k) E_s^H(f_o)$, respectively.

Using the focusing matrix in (15), the array output vector $\mathbf{X}(f_k)$ is transformed into a new vector,

$$\mathbf{Y}(f_k) = T(f_k) \mathbf{X}(f_k), \quad k = 1, 2, \dots, K. \quad (16)$$

From (9) and (16), we can get the smoothed spectrum density matrix as

$$R_Y = \sum_{k=1}^K (T(f_k) \mathbf{A}(\theta, f_k) P_S(f_k) \mathbf{A}^H(\theta, f_k) T^H(f_k) + \sigma^2(f_k) T(f_k) P_n(f_k) T^H(f_k)). \quad (17)$$

Now, we discuss the SSF method for the incoherent and coherent sources, respectively.

Incoherent Sources

For incoherent sources, we know that $\text{span}\{e_1(f_k), \dots, e_q(f_k)\} = \text{span}\{a(\theta_1, f_k), \dots, a(\theta_q, f_k)\}$. Therefore, we can get the relationship

$$E_s(f_k) = \mathbf{A}(\theta, f_k) \mathbf{B}(f_k). \quad (18)$$

In (18), $\mathbf{B}(f_k)$ is a $q \times q$ matrix and $\text{rank} \mathbf{B}(f_k) = q$. The column vector $b_i(f_k)$ of matrix $\mathbf{B}(f_k)$ is given by

$$b_i(f_k) = \frac{P_S(f_k) \mathbf{A}^H(\theta, f_k) e_i(f_k)}{\lambda_i(f_k) - \sigma^2(f_k)},$$

where $\lambda_1 \geq \lambda_2 \geq \dots \geq \lambda_q \geq \lambda_{q+1} = \dots = \sigma^2(f_k)$, are the

eigenvalues of $P_X(f_k)$ in descending order. Similarly, we get the relationship between $E_s(f_o)$ and $A(\theta, f_o)$ as

$$E_s(f_o) = A(\theta, f_o)B(f_o). \quad (19)$$

Using (13), (18) and (19), the smoothed spectrum density matrix R_Y in (17) becomes

$$R_Y = A(\theta, f_o)R_S A^H(\theta, f_o) + \sigma^2 R_\eta, \quad (20)$$

where

$$R_S = \sum_{k=1}^K B(f_o)B^{-1}(f_k)P_S(f_k)(B(f_o)B^{-1}(f_k))^H,$$

and

$$R_\eta = \sum_{k=1}^K \frac{\sigma^2(f_k)}{\sigma^2} T(f_k)P_\eta(f_k)T^H(f_k).$$

Similar to the CSM, the wideband source location can be achieved by using the smoothed spectrum density matrix R_Y in (20) with one of the several narrow-band spectrum estimation methods designed to operate at the focusing frequency f_o .

Coherent Sources

However, the above SSF is effective only for the incoherent sources. As to the coherent sources, the spatial-smoothing technique [7], proposed to decorrelate the coherence of narrow-band sources, may be applied in the SSF for the estimation of coherent wideband sources. For example, divide the array into M overlapped subarrays. The spatial-smoothed spectrum density matrix is formed by

$$\bar{P}_x(f_k) = \frac{1}{M} \sum_{i=1}^M P_{x_i}(f_k), \quad (21)$$

where $P_{x_i}(f_k)$ is the spectrum density matrix of the i th subarray. Hence, modify the SSF with $P_x(f_k)$ replaced by $\bar{P}_x(f_k)$ for M coherent sources estimation.

Projection Method

Furthermore, the construction of focusing matrix $T(f_k)$ in (15) requires performing eigendecomposition on the spectrum density matrix $P_X(f_k)$, which will increase the computation complexity of the SSF. To reduce the computation load for the SSF, the technique of simple computation of projection matrix [8] is suggested to estimate the signal subspace. When the source number is known a priori, we can choose q columns (or rows) from the spectrum density matrix $P_X(f_k)$, which are $u_i(f_k)$, $i = 1, \dots, q$. In order to achieve good performance, the chosen q columns are widely

spread so that they are well separated in the vector space. Those q vectors $u_i(f_k)$ are further orthogonalized by the Gram-Schmidt orthogonalization procedure and get q new vectors $u'_i(f_k)$. Thus, the projection matrix $Q(f_k)$ can be formed by

$$Q(f_k) = [u'_1(f_k), u'_2(f_k), \dots, u'_q(f_k)]. \quad (22)$$

Yeh [8] has shown that the columns of $Q(f_k)$ span the same signal subspace as $P_X(f_k)$. Therefore, with the projection matrix Q , the minimization problem of SSF in (14) is modified as

$$\min_{T(f_k)} \|Q(f_o) - T(f_k)Q(f_k)\|_F, \quad k = 1, 2, \dots, K, \quad (23)$$

subject to

$$T^H(f_k)T(f_k) = I.$$

By the above procedure, we can alleviate the computation burden in constructing the focusing matrix of the SSF. However, the projection method requires the a priori information on the number of sources. When source number is unknown, we can estimate the source number by information theoretic criteria, for example, by the methods based on the AIC [9] or MDL [10] criteria.

SIMULATION RESULTS

Computer simulations of both the CSM and the SSF are presented in this section. In simulations, the rotational signal-subspace (RSS) focusing matrix was used for the CSM. And the focusing angles were estimated by the delay-and-sum beamformer preliminarily for the CSM. We consider a linear array of sixteen sensors with equal spacing of half-wavelength at central frequency 100 Hz. The source signals were band-pass zero-mean white Gaussian processes with same central frequency 100 Hz and band-width 40 Hz. 100 snapshots were used, and for each snapshot, 33 frequency components of array output were obtained via DFT.

The simulation was first performed for the case of uncorrelated sources in multi-group scenario. The sources were distributed at 10° , 13° , 30° and 37° with equipower SNR=10 dB. Fig. 1 shows that the SSF is much effective in the estimation of DOAs of wideband sources in multi-group scenario. Next, we considered the case of multiple arrivals falling in one group. Four uncorrelated sources were located 9° , 12.5° , 16° and 35° , and the first three sources belongs to one group. Fig. 2 shows the resolution property of the SSF is better than the CSM for the case of multiple arrivals

Fig. 1. Spatial spectrum for multi-group signals (a) CSM, (b) SSF. A sixteen-element spaced linear array with half-wavelength spacing illuminated by four signals located at 10° , 13° , 30° and 37° with SNR=10dB.

within one group. Then, the statistics analysis for the SSF was estimated by 100 independent Monte Carlo trials. Four uncorrelated sources with SNR=10 dB were located at 10° , 15° , 30° and 35° . The bias, standard deviation (std) and mean square error (MSE) were listed in Table 1 at various SNRs. In the table, CSM⁽¹⁾ indicated the CSM with good focusing angles 12.5° and 32.5° , and CSM⁽²⁾ represented the CSM with focusing angles estimated by the delay-and-sum beamformer. Table 1 shows that CSM⁽¹⁾ has lower bias and standard deviation than CSM⁽²⁾, which indicates the sensitivity problem of the CSM. Also, we can observe that the performance of the SSF becomes better as the SNR increases. The result is reasonable since the estimation of signal subspace is more accurate for larger SNR. However, the bias of the SSF shown in Table 1 is still lower than that of the CSM.

Fig. 2. Spatial spectrum for multiple sources within one group. (a) CSM, (b) SSF. Simulation scenario as Fig. 1. Four signals located at 9° , 12.5° , 16° and 35° with SNR=10dB. Five independent simulation trials.

Finally, the simulation was carried out for coherent sources. In the simulation, the array was divided into 2 subarrays with 15 element sensors each. Four sources were located at -50° , -10° , 20° and 25° and the last two signals $s_3(t)$ and $s_4(t)$ were coherent with $s_4(t) = s_3(t - 0.125s)$. Fig. 3 validates the performance of SSF for coherent sources.

CONCLUSIONS

In this paper, we have proposed a new SSF method for the DOA estimation of wideband sources. The SSF transforms the signal subspace at each frequency bin onto the focusing subspace by using focusing matrices. The focusing matrix is formed without a priori knowledge of source angles. Thus, the SSF avoids the sensitivity problem caused by

Table 1. Statistical analysis for CSM and SSF. Four signals located at 10°, 15°, 30° and 35° and SNR=10dB.

$\theta=10^\circ$									
SNR	CSM ⁽¹⁾			CMS ⁽²⁾			SSF		
	Bias	std.	MSE.($\times 10^{-2}$)	Bias	std.	MSE.($\times 10^{-2}$)	Bias	std.	MSE.($\times 10^{-2}$)
0dB	0.0260	0.0101	0.0784	0.1252	0.1669	4.3528	0.0228	0.0855	0.7833
5dB	0.0265	0.0069	0.0748	0.1117	0.1387	3.1708	0.0032	0.0517	0.2682
10dB	0.0269	0.0047	0.0747	0.0799	0.0731	1.1716	0.0018	0.0271	0.0737
15dB	0.0273	0.0040	0.0761	0.0997	0.0773	1.5910	0.0005	0.0167	0.0280
20dB	0.0266	0.0047	0.0732	0.1079	0.1310	2.8808	0.0011	0.0088	0.0079

$\theta=15^\circ$									
SNR	CSM ⁽¹⁾			CMS ⁽²⁾			SSF		
	Bias	std.	MSE.($\times 10^{-2}$)	Bias	std.	MSE.($\times 10^{-2}$)	Bias	std.	MSE.($\times 10^{-2}$)
0dB	-0.0455	0.0088	0.2146	-0.0719	0.1163	1.8702	0.0230	0.0925	0.9091
5dB	-0.0445	0.0060	0.2013	-0.0627	0.1245	1.9428	-0.0094	0.0528	0.2876
10dB	-0.0438	0.0041	0.1931	-0.0583	0.0972	1.2840	0.0024	0.0300	0.0905
15dB	-0.0435	0.0039	0.1904	-0.0684	0.1183	1.8687	-0.0002	0.0170	0.0291
20dB	-0.0434	0.0037	0.1898	-0.0759	0.1095	1.7744	-0.0019	0.0084	0.0073

$\theta=30^\circ$									
SNR	CSM ⁽¹⁾			CMS ⁽²⁾			SSF		
	Bias	std.	MSE.($\times 10^{-2}$)	Bias	std.	MSE.($\times 10^{-2}$)	Bias	std.	MSE.($\times 10^{-2}$)
0dB	0.0504	0.0113	0.2663	0.1518	0.1648	5.0190	-0.0013	0.0571	0.3266
5dB	0.0498	0.0071	0.2535	0.1086	0.1225	2.6806	-0.0058	0.0333	0.1141
10dB	0.0485	0.0052	0.2376	0.1418	0.1374	3.8986	0.0016	0.0175	0.0308
15dB	0.0480	0.0047	0.2330	0.1673	0.2137	7.3660	0.0014	0.0119	0.0144
20dB	0.0487	0.0045	0.2395	0.1229	0.1198	2.9464	0.0004	0.0065	0.0042

$\theta=35^\circ$									
SNR	CSM ⁽¹⁾			CMS ⁽²⁾			SSF		
	Bias	std.	MSE.($\times 10^{-2}$)	Bias	std.	MSE.($\times 10^{-2}$)	Bias	std.	MSE.($\times 10^{-2}$)
0dB	-0.0284	0.0137	0.0996	-0.2039	0.2456	10.1889	0.0125	0.0647	0.4340
5dB	-0.0320	0.0089	0.1104	-0.1744	0.2197	7.8690	0.0041	0.0368	0.1370
10dB	-0.0301	0.0050	0.0930	-0.1628	0.2138	7.2206	-0.0058	0.0219	0.0515
15dB	-0.0298	0.0053	0.0916	-0.1926	0.2138	8.2788	0.0004	0.0105	0.0110
20dB	-0.0300	0.0049	0.0923	-0.2047	0.2473	10.3070	-0.0001	0.0071	0.0051

CSM⁽¹⁾: the CSM with focusing angles 12.5° and 32.5°; CSM⁽²⁾: the CSM with focusing angles estimated by delay-and-sum beamformer

Fig. 3. Spatial spectrum for coherent signals (a) CSM, (b) SSF. Simulation scenario as Fig. 1. Four signals located at -5° , -10° , 20° and 25° with SNR=10dB. $s_3(t)$ and $s_4(t)$ are coherent, where $s_4(t) = s_3(t - 0.125s)$.

preliminary angle estimate. Simulations indicate the SSF is much effective in the wideband source estimation than the CSM, especially for the case of multi-group signals. And the resolution and the statistics performance of the SSF are better than those of the CSM.

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以信號子空間聚焦法進行寬頻訊號源方位估測

張麗娜 涂鐘範

國立台灣海洋大學商船學系

摘要

本論文提出一高解析度之信號子空間聚焦法進行寬頻同調訊號源之方位估測。此法乃利用一聚焦矩陣將不同頻率所對應之信號子空間轉換到中心（或聚焦）頻率上，形成一聚焦子空間，而後將高解析度之窄頻方位估測法用於此聚焦頻率上。此聚焦矩陣之形成不需預估方位，故信號子空間聚焦法可減緩因聚焦誤差所造成之估測偏差。電腦模擬驗證信號子空間聚焦法可有效估測寬頻同調訊號源之方位。