

[Volume 17](https://jmstt.ntou.edu.tw/journal/vol17) | [Issue 4](https://jmstt.ntou.edu.tw/journal/vol17/iss4) Article 9

SERVICE LIFE PREDICTION OF PIER FOR THE EXISTING REINFORCED CONCETE BRIDGES IN CHLORIDE-LADEN ENVIRONMENT

Ming-Te Liang Department of Civil Engineering, China Institute of Technology, Taipei 115, Taiwan, R.O.C., mtliang@cc.chit.edu.tw

Ran Huang Department of Harbor and River Engineeing, National Taiwan Ocean University, Keelung 20224, Taiwan, R.O.C.

Shen-An Feng Department of Harbor and River Engineeing, National Taiwan Ocean University, Keelung 20224, Taiwan, R.O.C.

Chi-Jang Yeh Sinotech Engineering Consultants Ltd., Taipei 105, Taiwan. R.O.C

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Recommended Citation

Liang, Ming-Te; Huang, Ran; Feng, Shen-An; and Yeh, Chi-Jang (2009) "SERVICE LIFE PREDICTION OF PIER FOR THE EXISTING REINFORCED CONCETE BRIDGES IN CHLORIDE-LADEN ENVIRONMENT," Journal of Marine Science and Technology: Vol. 17: Iss. 4, Article 9.

DOI: 10.51400/2709-6998.1988

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Acknowledgements

The authors wish to thank the financial support of the National Science Council under contract NSC-95-2221-E-157-007.

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Ming-Te Liang*, Ran Huang**, Shen-An Feng**, and Chi-Jang Yeh***

Key words: bridge, corrosion, pier, reinforced concrete, service life prediction.

ABSTRACT

The prediction method of service life for bridge structures is played an important role of bridge management system. In this paper, the mathematical modeling was to study the servise life prediction of pier for existing reinforced concrete (RC) bridge exposed to chloride environment. The corrosion process has three stages, the initiation time (t_c) , the depassivation time (t_p) , and the corrosion (propagation) time (t_{corr}) . The total service life of pier for the existing RC bridge can be expressed as $t = t_c + t_p + t_{corr}$. Many mathematical models were applied to predicting each value of the t_c , t_p , and t_{corr} . The Fick's second law, the average of Bazant and Proposed methods, and the modified Bazant method are suggested to estimate the values of *tc*, *tp*, *tcorr*, respectively. The Tzyh-chyang and Dah-duh RC bridges in Taiwan were provided illustrative examples for the modeling approaches and service life of predictions. The predicted results used mathematical models may be reasonable for the pier service life of the existing Tzyh-chyang and Dah-duh RC bridges. The results of present study may help to offer a basis for repair, strengthening, and demolition of existing RC bridges.

I. INTRODUCTION

In the important infrastructure in any country, concrete and reinforced concrete (RC) is one of the most widely used construction materials all over the world. Many building, housing, and industrial structures are constructed of RC. Most infrastructures make use of concrete extensively, such as dams,

airports, coastal embankments, thermal power or nuclear energy plant, road and railway bridges, harbors and wharfs. Nevertheless, if these structures are exposed long-term to a bad environment which is of chloride ions, or carbon dioxide, or sulfate dioxide, then their service lives will be reduced. The safety of concrete or RC structures during employment needs to be taken into consideration. Moreover, the durability of concrete or RC structures have to be investigated. A worthwhile subject for study would be to set up firmly a complete evaluation method for reasonally calculating the service life of RC structures and for exactly furnishing judgment for repair, stengthening, or demolition.

A great deal of literature about the service life prediction for building materials and components, concrete, and RC structures was made a summary by Liang *et al.* [14]. However, some literature pertinent to this acticle should be introduced. Bazant [2, 3] built a simple and important physical model for steel corrosion in concrete. On the basis of Bazent's theory, the RC corrosion problem can be formed as an initial-boundaryvalue problem with mathematical equation. Accroding to the theory of elasticity, Bazent established two classical formulas for calculating depassivation time (t_p) and corrosion (or propagation) time (t_{corr}). The depassivation time is defined as depassivation normally provided to the steel by the alkaline hydrated cement matrix is destroyed locally loading to pitting corrosion. The corrosion time extends from the time when corrosion products form to the stage where they generate sufficient stress to disrupt the concrete cover by cracking or spalling, or when local attack on the reinforcement becomes sufficiently severe to impair its load-carrying capacity. It is worthy to point out that based on corrosion control Bazant derived the t_p formula by a parabolic a parameter Cl^- concentration. Furthermore, Liang *et al.* [14] pointed out that the parameter ΔD (increment of steel diameter) in formula of *t*_{corr} derived by Bazent [3] has been made a mistake. Liang *et al.* [14] have offered the accurete formula and called the modified Bazant method.

Cady and Weyers [5] employed Bazant's model to evaluate the time to deterioration initiation, deterioration rate, and the time to rehabilitation for concrete bridge decks. They pointed out that the time to cracking has ranged between two and five

Paper submitted 04/09/08; accepted 12/13/08. Author for correspondence: Ming-Te Liang (e-mail: mtliang@cc.chit.edu.tw).

^{}Department of Civil Engineering, China Institute of Technology, Taipei 115, Taiwan, R.O.C.*

*^{**}Department of Harbor and River Engineeing, National Taiwan Ocean University, Keelung 20224, Taiwan, R.O.C.*

*^{***}Sinotech Engineering Consultants Ltd., Taipei 105, Taiwan. R.O.C.*

Fig. 1. Issues related to service life prediction.

years. Subramanian and Wheat [20] used Bazant's model to predict time of t_p in a chloride environment. Liu and Miau [16] predicted the t_p , the corrosion cracking time, the breaking time of bond between concrete area steel, and the steel area losing time according to the Bazant model. Clifton [6, 7, 8] pointed out that the five methods of expenience, deduction, accelerated testing, mathematical modeling, reliability, and stochastic concept can be used to predict the service life of concrete. On the basis of Fick's second law of linear diffusion, Weyers [22] derived a practical formula for calculating the time-to-initiate corrosion. On the authority of elesticity, Liu [17] and Liu and Weyers [18] established an empirical formula for calculating the time-to-cracking. The corrosion-cracking model is dependent on the cover depth, properties of the concrete and steel/concrete interface, type of corrosion products, and the size of the reinforcing steel and is a function of the critical weight of rust products and corrosion rate. Boddy *et al.* [4] provided issues related to service life prediction as sketched in Fig. l.

Although these studies have provided much valuable application on the service life prediction for the concrete or RC structures to date, no theoretical studies have been carried out concerning the depassivation time derived by linear relation

for the chloride concentration. The purpose of this paper was to estimate the service lives of piers for two existing RC bridges in chloride-laden environments using several mathematical models. The result of present study may provide a useful reference for repair, strengthening and demolition of existing RC bridges.

II. ELECTROCHEMICAL PROCESSES CAUSING CHLORIDE-ION INGRESS

When the concrete or RC structures were contaminated by the chloride-ion, they were reduced the alkalinity of the water solution in the pores of concrete. This can be caused by water dilution that accompanies cracking. Moreover, the whole or partial passive film around the steel surface would be broken or depassivated. The steel surface at different positions will make a potentially large difference and form anode and cathode as an electrochemical cell which is a kind of electrochemical process. Based on a common sense, under the constant environment of oxide and water, the steel are going to corrosion. Generally speaking, the corrosion type is a sort of streak. This implies that corrosion distributes itself on a large area of steel surface. Nevertheless, the corrosion depth is not large due to concrete with the high alkalinity environment. The corrosion process can be described by chemical reaction. The electrode reaction can be expressed as [2]

$$
Fe \rightarrow Fe^{2+} + 2e^-
$$
 (at anode surface)

$$
O_2 + 2H_2O + 4e^- \rightarrow 4OH^-
$$
 (at cathode surface)

where e^- = election.

The next chemical processes at the anode surface are

$$
Fe^{2+} + 2OH^- \rightarrow Fe(OH)_2 \text{ (anode)}
$$

$$
4Fe(OH)_2 + O_2 + 2H_2O \rightarrow 4Fe(OH)_3 \text{ (anode)}
$$

Failure may occur due to corrosion damage. If undergone of the steel bars is large (say, $s > 6D$, $D =$ steel diameter), we may propose that the failure mode is made up of planar cracks of 45° inclination, emanating from opposite points on the surface of the steel bar. This phenomenon was described by Bazant [2] and Liang *et al*. [14].

III. PREDICTION METHOD OF SERVICE LIFE

The deterioration process of RC structure undergone corrosion media attack is sketched in Fig. 2 [21]. The corrosion processes in Fig. 2 are regarded as three stages, initiation time (t_c) , depassivation time (t_p) , and corrosion (or propagation) time (t_{corr}) . The initiation time is defined as the time for chloride ions to penetrate from the concrete surface to the surface

Time	Prediction method	Formula	Reference			
	Fick's 2nd Law	$C(x,t) = C_o$ erfc $\frac{x}{\sqrt{4D_c t_c}}$	Crank [11]			
	Guirguis	$t_c = \frac{L}{\lambda D}$	Guirguis [12]			
	Hookham	$t_c = K_c K_c x^2 + K_a x$	Hookham [13]			
Initiation time, t_c	AJMF	$C(x,t) = kt \left \left(1 + \frac{x^2}{2D_c t}\right) \text{erfc}\left(\frac{x}{2\sqrt{D_c t}}\right) \left(\frac{x}{\sqrt{\pi D_c t}}\right) \text{e}^{-\frac{x^2}{4D_c t}} \right $ $C(x,t) = k\sqrt{t} \left\{ e^{\frac{x^2}{4D_c t}} - \left[\frac{x\sqrt{\pi}}{2\sqrt{D_c t}} erfc\left(\frac{x}{2\sqrt{D_c t}}\right) \right] \right\}$	Amey et al. [1]			
Depassivation time, t_p	Bazant	$t_p = \frac{1}{12D_c} \left \frac{L}{1 - \sqrt{\frac{C^*}{C}}} \right $	Bazant [3]			
	Proposed	$t_p = \frac{1}{4D_c} \left(\frac{L}{1 - \sqrt{\frac{C^*}{C}}} \right)$	Proposed			
	ME	$t_{corr} = \frac{\delta \rho_{st} Z F}{\Delta t}$	Mangat and Elgarf [19]			
	Bazant	$t_{corr} = \rho_{cor} \frac{D \Delta D}{s}$, $\Delta D = 2 f'_i 2 \frac{L}{D} \delta_{pp}$	Bazant [2]			
Propagation time, t_{corr}	Modified Bazant	$t_{corr} = \rho_{cor} \frac{D}{s} \frac{\Delta D^*}{i}, \ \Delta D^* = f_t \left[2 \left(\frac{L}{D} + 1 \right) \middle \delta_{pp} \right]$	Liang et al. [14]			
	CW	$t_{corr} = 2 - 5$ years	Cady and Weyers [5]			
	Weyers	$t_{corr} = \frac{W_{crit}^2}{2k_n}$	Weyers [22]			

Table l. Prediction method for corrosion initiation, depassivation, and propagation time.

of the passive film. The degree of deterioration (i.e., ordinate), *Dd*, in Fig. 2 can be defined as

$$
D_d = 1 - \frac{x}{10} \tag{1}
$$

where x is the integrity of RC structure. The value of x ranges from zero to ten. For instance, if the RC structure is free of corrosion damage then the value of *x* is ten. Thus, the degree of deterioration is zero.

The total service life of RC structures can be expressed in terms of

$$
t = t_c + t_p + t_{corr} \tag{2}
$$

Fig. 2. Deterioration Process of reinforced concrete structures due to corrosion.

Table 2. Overall structural conditions of Tzyh-chyang bridge.

According to (2) and using the values of t_p , t_c , and t_{corr} , we can predict the service life of RC structures. The prediction method for t_p , t_c , and t_{corr} , are listed in Table 1.

In Table 1, we provide a proposed method for calculating the depassivation time t_p . In this study, the chloride concentration is considered as the mechanism of corrosion control. Hence, the variable of permeability depth can be expressed as a declined straight line. The derivation process is stated in detail in the Appendix.

IV. ILLUSTRATIVE EXAMPLES

The safe evaluation of an existing bridge alter being constructed 10 years is an important work for an infrastructure or bridge management system. Rule specification, and systems

for safe evaluation have been set up in many countries. In this study, the mathematical models for service life predicition mentioned earlier are used to evaluate the service lives of Tzyh-chyang and Dah-duh RC bridges m Taiwan. Tables 2 and 3 show the overall structural conditions of Tzyh-chyang and Dah-duh bridges, respectively. According to CNS-1238 [10], concrete specimens were cored in-situ. Based on CNS-1232 [9], the compressive strength of the concrete specimens were determined and are listed in Table 4.

In this study, many parameters should be well known for using the mathematical models mentioned in Table 1 to calculate the service lives of the Tzyh-Chyang and Dah-duh bridges. Nevertheless, except the steel diameter $D = 19$ mm, the compressive strength, f_c' (Table 4), tensile strength f_t' (Table 4), elastic modulus, E_c (Table 4), and the effective elastic modulus, E_{ef} (Table 4), of the concrete, corrosion current density, *icorr* (Tables 5 and 6), and cover thickness, *L* (Tables 5 and 6), were supplied in the report. Other parameters were required as follows: the diffusion coefficient of chloride ions, $D_c = 77$ mm^2 /year = 2.44 \times 10⁻⁶ mm²/s, the threshold value of the chloride concentration, $C^* = 8 \text{ kg/m}^3$, the concentration of chloride ions in pores of concrete at the surface, $C_0 = 25 \text{ kg/m}^3$, the value of concrete, $\lambda = 1.0 \times 10^{-2}$, creep coefficient of concrete, ϕ_{cr} = 2.0 [3], poisson's ratio, v_c = 0.18 [3], the rate of rust production per unit area of plane, $j_r = 1.5 \times 10^{-15}$ g/m²-s [3], the density of the corrosion product, $\rho_{cor} = 3600 \text{ kg/m}^3 = 3.6 \text{ g/cm}^3$ [3], the space of the steel bar, $s = 10$ cm, and the thickness of

Bridge	Test Point No.	Test Point	Compressive strength $f'_c\left(\frac{kgf}{cm^2}\right)$	Average compressive strength $f'_c(MPa)$	Tensile strength $f'_t(MPa)$	Average tensile Elastic strength modulus $f'_t(MPa)$ $E_c(GPa)$		Effective elastic modulus E_{ef} (GPa)		
	$\mathbf{1}$	$P3-1-1$	263		2.82		23.87	7.96		
	$\mathfrak{2}$	P13-2-1	212		2.53		21.43	7.14		
	3	$P17-2-1$	414		3.54		29.94	9.98		
	$\overline{4}$	P22-2-2	372		3.36		28.38	9.46		
Tzyh-	5	$P26-2-1$	398	29.97	3.47	3.03	29.36	9.79		
chyang	6	P29-2-2	253		2.77		23.41	7.8		
	7	$P32-1-1$	281		2.92		24.67	8.23		
	8	$P36-1-1$	328		3.15		26.65	8.88		
	9	P40-2-2	280		2.91		26.62	8.21		
	$10\,$	P44-2	256		2.79		23.55	7.85		
	\mathbf{A}	$P1-3$	219		2.58		21.78	7.26		
	B	$P3-2$	234		2.66		22.51	7.5		
	C	$P14-2$	196		2.44		20.6	6.87		
	${\bf D}$	P15-3	239		2.69		22.75	7.58		
	$\mathbf E$	P16-2	248		2.74		23.18	7.73		
Dah-duh	\mathbf{F}	P17-2	222	23.42	2.59	2.79	21.93	7.31		
	G	P18-3	185		2.37		20.01	6.67		
	H	P19-3	342		3.22		27.22	9.07		
	Ι	$P20-2$	380		3.39		28.69	9.56		
	$\bf J$	P21-3	334		3.18		26.9	8.97		

Table 4. Compressive strength and properties of Tzyh-chyang and Dah-duh bridges in Taiwan.

Remark: 1. $1MPa = 1N/mm^2 = 10.2 kg f/cm^2$. 2. $f'_t = 0.087 f'_c$. 3. $E_c = 4700 (f_c)^{\frac{1}{2}}$ $E_c = 4700 (f_c')^2 MPa.$ 4. $E_{ef} = E_c / (1 + \phi_{cr}), \phi_{cr} = 2.0.$

pore band around the steel/concrete interface, $d_0 = 12.5 \text{ }\mu\text{m} =$ 12.5×10^{-3} mm. Inserting these given and suppose parameters into the formulas of Table 1, the values of t_c , t_p , and t_{corr} for the Tzyh-chyang and Dah-duh bridges were calculated and listed in Tables 5 and 6, respectively. It is worthy to point out that the computer package, i.e., Mathematica [23], should be employed to calculate the values of t_c from the Fick second law and AJMF methods. Note that the average value of t_{corr} based on the CW method [5], was adopted in this investigation, i.e, t_{corr} = 3.5 years (Tables 5 and 6). According to (2), the maximum and minimum service lives for each pier of the Tzyhchyang and Dah-duh bridges are listed in Tables 5 and 6, i.e., $t_{\text{max}} = t_{c, \text{max}} + t_{p, \text{max}} + t_{corr, \text{max}}$ and $t_{\text{min}} = t_{c, \text{min}} + t_{p, \text{min}} + t_{corr, \text{min}}$ respectively.

V. DISCUSSION

In this paper the service lives of piers for the two existing RC bridge exposed to chloride environment were calculated

by using the mathematical models. A new formula has been proposed for calculating the depassivation time (t_p) . The findings indicate that service life of existing RC bridge can be predicted.

In such measure of t_c values from Tables 5 and 6, the results calculated from the Guirguis, AJMF (1) and AJMF (2) were very approached. The results of t_c obtained from the Hookham method are larger than $2.4 \sim 2.5$ times those results of t_c gained from the method of Fick's second law. The results of t_c obtained from the AJMF method (1) is larger than $4\%~8\%$ times those results obtained from the AJMF method (2). Since the Hookham method concerns parameters related to the concrete cover thickness, the predicted values for t_c are larger than those results obtained by the other methods. The predicted maximum values for service life, t_{max} were based on the Hookham method.

In the case of *t* values from Tables 5 and 6, the results predicted by the proposed method were larger than 3 times those results of t_p calculated by the Bazant method. This difference

Test	Corrosion current	Cover	t_c (yrs)					t_p (yrs)		t_{corr} (yrs)					Service life Prediction (yrs)	
point No.	density $i_{corr} (\mu A/cm^2)$	thickness L (mm)	Fick's 2nd law	Guirguis method	Hookham method	(1) $k = 0.1$	AJMF method (2) $K = 0.545$	Bazant method	Proposed method	ME method	Bazant method	Modified method	CW method	Weyers method	$t_{\rm max}$	t_{\min}
	0.12	50	39.5	64.94	181,29	66.19	61.35	14.34	43.02	31.01	7.96	9.47	3.5	37.44	261.75	57.34
2	0.05	50	39.5	64.94	181.29	66.19	61.35	14.34	43.02	74.44	7.96	9.47	3.5	89.86	314.17	57.34
3	0.05	50	42.25	64.94	181.29	71.59	66.93	14.34	43.02	74.44	7.96	9.47	3.5	89.86	314.17	60.09
4	0.02	50	39.5	64.94	181.29	66.19	61.35	14.34	43.02	186.10	7.96	9.47	3.5	224.65	448.96	57.34
5	0.03	50	45.13	64.94	181.29	77.56	72.92	14.34	43.02	124.07	7.96	9.47	3.5	149.77	374.08	62.97
6	0.07	50	39.5	64.94	181.29	66.19	61.35	14.34	43.02	53.17	7.96	9.47	3.5	64.19	288.5	57.34
	0.06	50	39.5	64.94	181,29	66.19	61.35	14.34	43.02	62.03	7.96	9.47	3.5	74.88	299.19	57.34
8	0.06	50	39.5	64.94	181.29	66.19	61.35	14.34	43.02	62.03	7.96	9.47	3.5	74.88	299.19	57.34
9	0.05	50	39.5	64.94	181.29	66.19	61.35	14.34	43.02	74.44	7.96	9.47	3.5	89.86	314.17	57.34
10	0.02	50	45.91	64.94	181.29	79.14	74.57	14.34	43.02	186.10	7.96	9.47	3.5	224.65	448.96	63.75
										Average	336.31	58.52				

Table 5. Service life prediction of Tzyh-chyang bridge.

Table 6. Service life prediction of Dah-duh bridge.

Test	Corrosion current density No. i_{corr} (μ A/cm ²)	Cover thickness L (mm)	t_c (yrs)					t_p (yrs)		t_{corr} (yrs)					Service life Prediction (yrs)	
point			Fick's 2nd law	Guirguis method	Hookham method	AJMF method (2) (1)		Bazant method	Proposed method	ME method	Bazant method	Modified method	CW method	Weyers method	$t_{\rm max}$	t_{\min}
						$k = 0.1$	$K = 0.545$									
A	0.23	40	41	51.94	119.22	69.23	64.38	9.18	27.54	16.18	7.24	8.77	3.5	19.53	166.29	53.68
B	0.05	40	41	51.94	119.22	69.23	64.38	9.18	27.54	74.44	7.24	8.77	3.5	89.86	236.62	53.68
C	0.2	40	50.13	51.94	119.22	87.72	83.69	9.18	27.54	18.61	7.24	8.77	3.5	22.47	169.23	62.81
D	0.11	40	43.33	51.94	119.22	73.89	69.13	9.18	27.54	33.84	7.24	8.77	3.5	40.85	187.61	56.01
E	0.33	40	45.91	51.94	119.22	79.14	74.57	9.18	27.54	11.28	7.24	8.77	3.5	13.62	160.38	58.59
F	0.07	40	45.13	51.94	119.22	77.56	72.92	9.18	27.54	53.17	7.24	8.77	3.5	64.19	210.95	58.59
G	0.05	40	41	51.94	119.22	69.23	64.38	9.18	27.54	74.44	7.24	8.77	3.5	89.86	236.62	53.68
H	0.06	40	39.5	51.94	119.22	66.19	61.35	9.18	27.54	62.03	7.24	8.77	3.5	74.88	221.64	52.18
	0.05	40	42.25	51.94	119.22	71.73	66.89	9.18	27.54	74.44	7.24	8.77	3.5	89.86	236.62	54.93
	0.04	40	43.33	51.94	119.22	73.89	69.13	9.18	27.54	93.05	7.24	8.77	3.5	112.33	259.09	56.01
														Average	208.51	56.02

is caused by the different declined mechanisms of *Cl*[−] concentration. The proposed method uses a declined straight line while the Bazant method uses a declined parabolic curve. However, the real phenomenon may be that first the declined parabola curve occurs and then the declined straight line does. Based on this situation, the suitable value of t_p is the average of results obtained by the proposed and Bazant methods.

In so far as t_{corr} values from Tables 5 and 6, the results estimated by the CW method were not supported by a theoretical formula. The results of t_{corr} obtained from the Weyers and ME methods were very similar. In addition, Liang *et al.* [15] pointed out that $t_c \approx 4$ $t_{corr} \sim 5$ t_{corr} . If this is reliable, then the values for *tcorr* obtained from the modified Bazant method coincide.

As a result, the Fick's second law, the average of proposed and Bazant methods, and the modified Bazant method are

suggested for estimating the values of t_c , t_p , and t_{corr} , respectively. Based on (2) and Tables 5 and 6, we may accept the results obtained from the service life prediction for the Tzyh-Chyang and Dah-duh bridges of 58.82 and 56.02 years in Taiwan, respectively. This means the service life prediction coincide with $t_{\min} \leq t \leq t_{\max}$.

The method presented here is accurate, but can not be implemented in steel bridge. Moreover, our findings may be valid only for chloride environment. We suggest that similar studies be conducted with general atmospheric environment.

VI. CONCLUDING COMMENTS

This study predicted the service lives of piers for existing RC bridges. A new method for estimating the depassivation time has presented. The service life model consists of three stages: initiation (diffusion) time, depassivation time, and corrosion (propagation) time. Among the method of Fick's second law, the average of proposed and Bazant methods, and the modified Bazant method are suggested to estimate the initiation, depassivation, and corrosion time, respectively. The results of this investigation may provide a basis for repair, strengthening, and demolition of existing RC bridges. The prediction method reported in this paper could be extended to applications for other existing RC bridges. For the sake of securing a correct prediction result, we recommend that the parameters used should be conducted in an experimented model first.

ACKNOWLEDGMENTS

The authors wish to thank the financial support of the National Science Council under contract NSC-95-2221-E-157-007.

APPENDIX

Bazant [2, 3] considered the concentration of *Cl*[−] , *C*, as a variable of permeability depth with parabolic curve (see Fig. 3) which is a kind of the mechanism of diffusion control. However, if the concentration of Cl ⁻ is referred as the mechanism of corrosion control, then the variable of permeability depth can be represented as a declined straight line as shown in Fig. 4. From Fig. 4, when penetration depth $x < H$, *C* can be expressed in terms of the similarity of triangle.

$$
C = C_o \left(1 - \frac{x}{H} \right), \ x < H \tag{3}
$$

Differentiating (3) with respect to *x*, we obtain

$$
\frac{\partial C}{\partial x} = -\frac{C_o}{H} \tag{4}
$$

Multiplying $-D_C$ to (4), we have

$$
-D_c \frac{\partial C}{\partial x} = D_c \frac{C_o}{H}
$$
 (5)

The total quality of chloride-ion in concrete can be expressed as in terms of

$$
M_C = \int_{0}^{H} C dx
$$
 (6)

Substituting (3) into (6) and integrating (6), we obtain

$$
M_c = \frac{C_o H}{2} \tag{7}
$$

Fig. 3. Parabolic relation between *C* **and** *x***.**

Differentiating (7) with respect to *t*, we have

$$
\frac{dM_C}{dt} = \frac{C_o}{2} \frac{dH}{dt} \tag{8}
$$

The flux of chloride-ion of (6) must equal *dM/dt* at penetration depth $x < 0$. Thus, we have

$$
\frac{dM}{dt} = D_c \frac{C_o}{H} \tag{9}
$$

Equation (8) is equal to (9) , i.e,

$$
\frac{C_o}{2} \frac{dH}{dt} = \frac{D_c C_o}{H}
$$
 (10)

After integrating to (10), we have

$$
t = \frac{1}{4D_c}H^2\tag{11}
$$

If chloride-ion penetrate on the steel surface, i.e, penetration depth $x =$ concrete cover *L*, then (3) can be changed as

$$
H = \frac{L}{\left(1 - \frac{C^*}{C_o}\right)}\tag{12}
$$

where C^* is the threshold of chloride concentration which is depassivated the anode surface of steel in concrete. Substituting (9) into (10), the depassivation time, t_p , can be derived as follows:

$$
t_p = \frac{1}{4D_c} \left(\frac{L}{1 - \frac{C^*}{C_o}} \right)^2
$$
 (13)

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